Harmonic Models

CS 275B/Music 254

General questions

- Can harmony be separated from pitch and rhythm?
- Should harmony be computed top-down or bottom up?
- How should harmonic change be segmented?
- How can harmonic information best be communicated?

Krumhansl on Rhythm and Pitch Organization

Psychological Bulletin (2000). 126/1, 159-179.

Rhythmic phenomena

- Periodic pulse
- Grouping
- Objective rhythmicization
- Ratios of durations
- Patterns of duration (rather than absolute values) of primary psych importance (*motoric involvement*)

Pitch phenomena

- Discreet frequencies
- Melodic intervals
- Consonance, dissonance
- Pitch patterns

Bottom-up approach

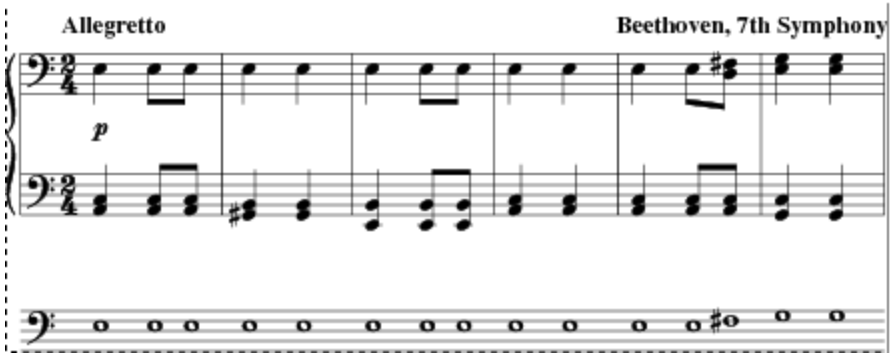
Krumhansl (2): Pitch aspects of harmony

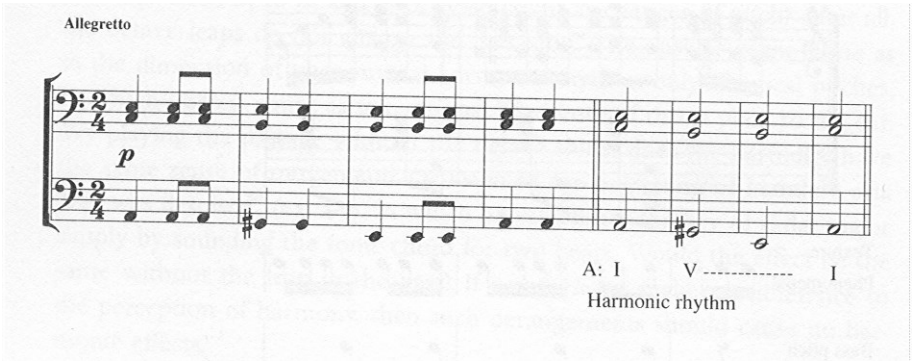
- Categorical perception of pitch (intervallic sizes)
- Tonal hierarchies
- Key estimation
- Virtual pitch (missing fundamental)
- Transposition (not always recognized)
- Modulatory distance (circle-of-fifths)
- Large-scale musical form

- *Conclusion:* musical patterns organized into hierarchies of events

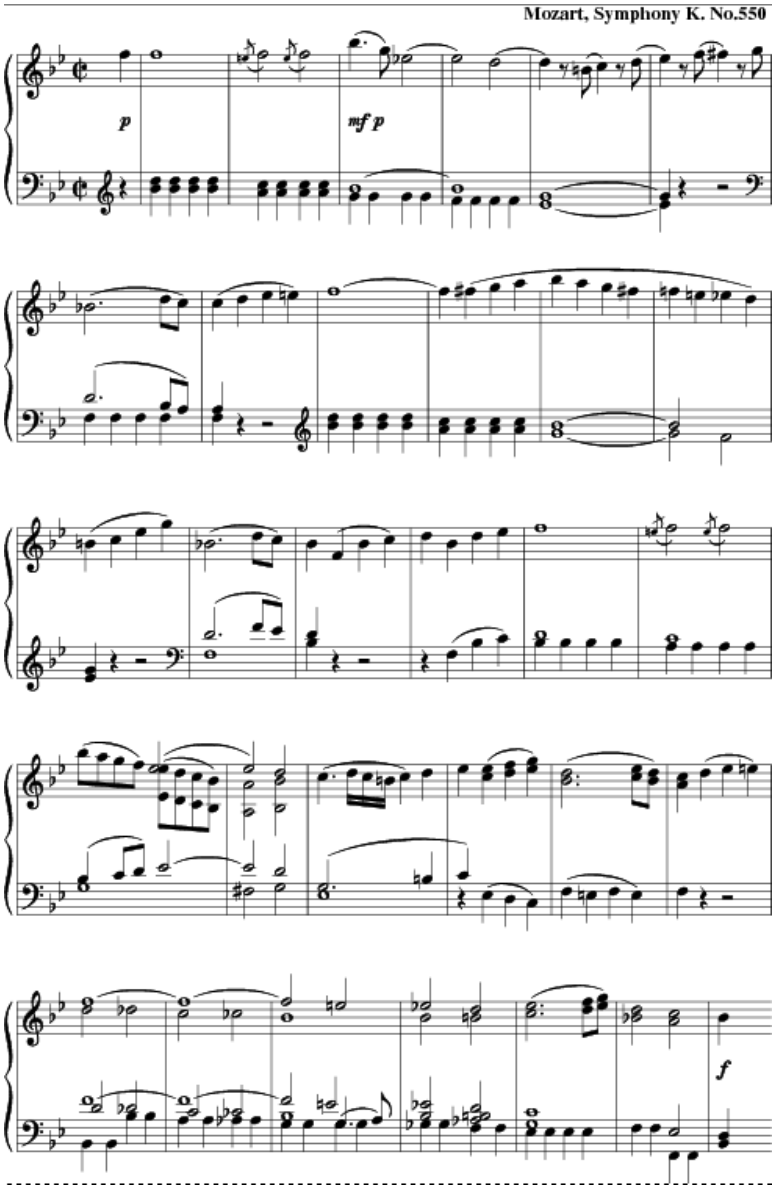
Melodic change vs. Harmonic change

1. Same melody, changing harmony





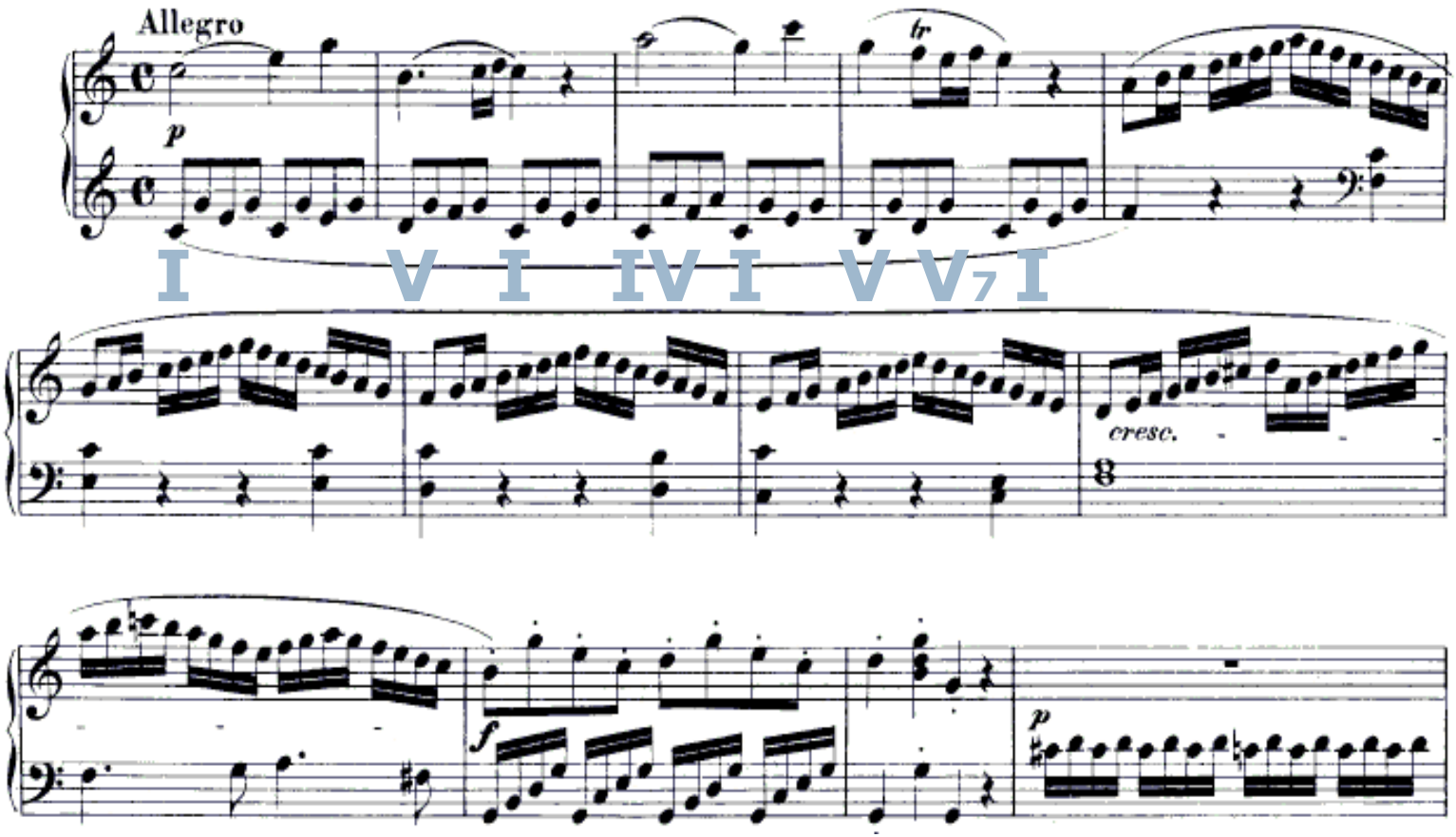
Dynamic properties of structure



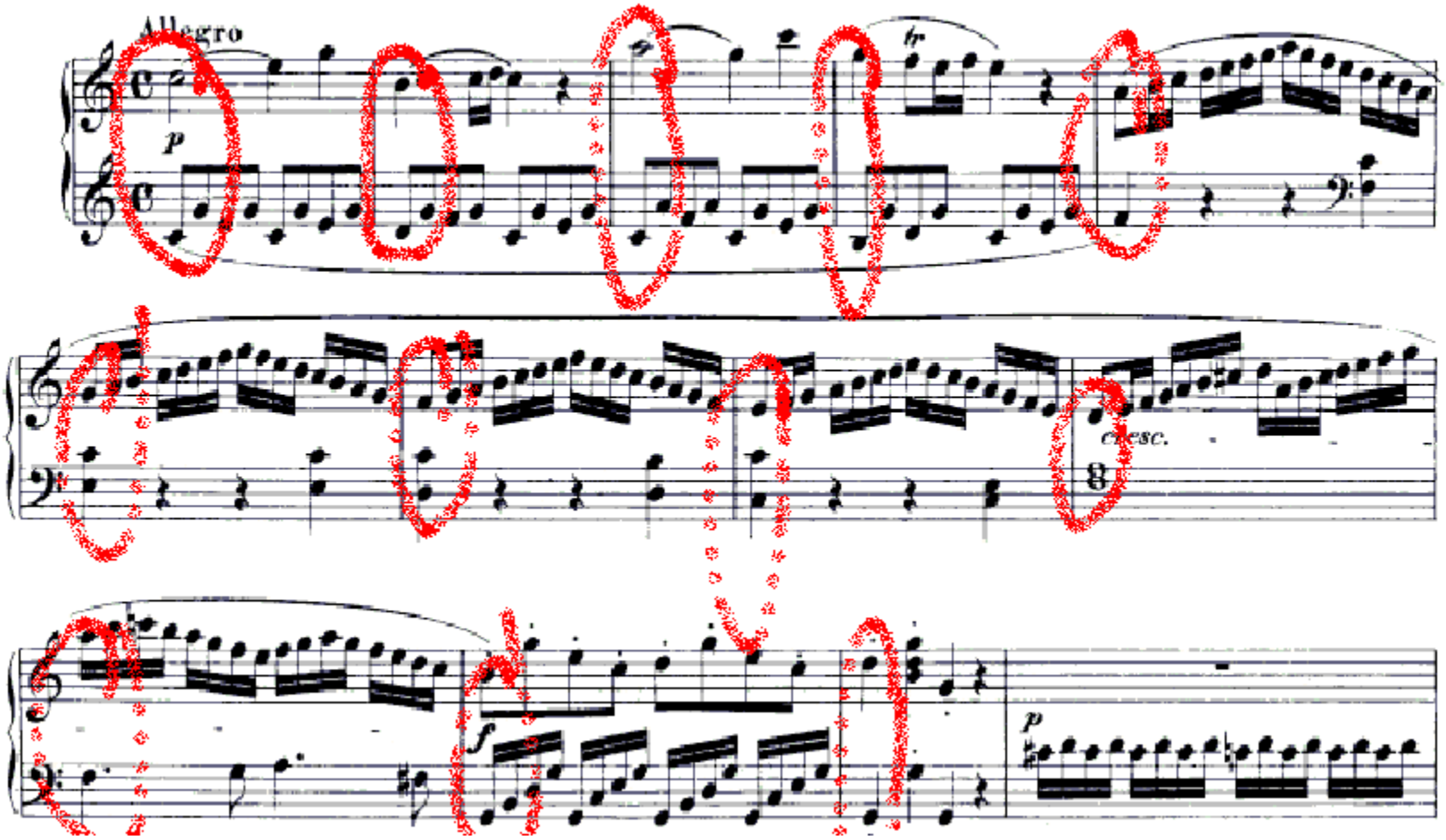
In regular circumstances

- How many times is the theme (re)stated?
- How many times is the melody the same?
- How many times is the harmony the same?

Hugo Riemann (Riemann-esque analysis)

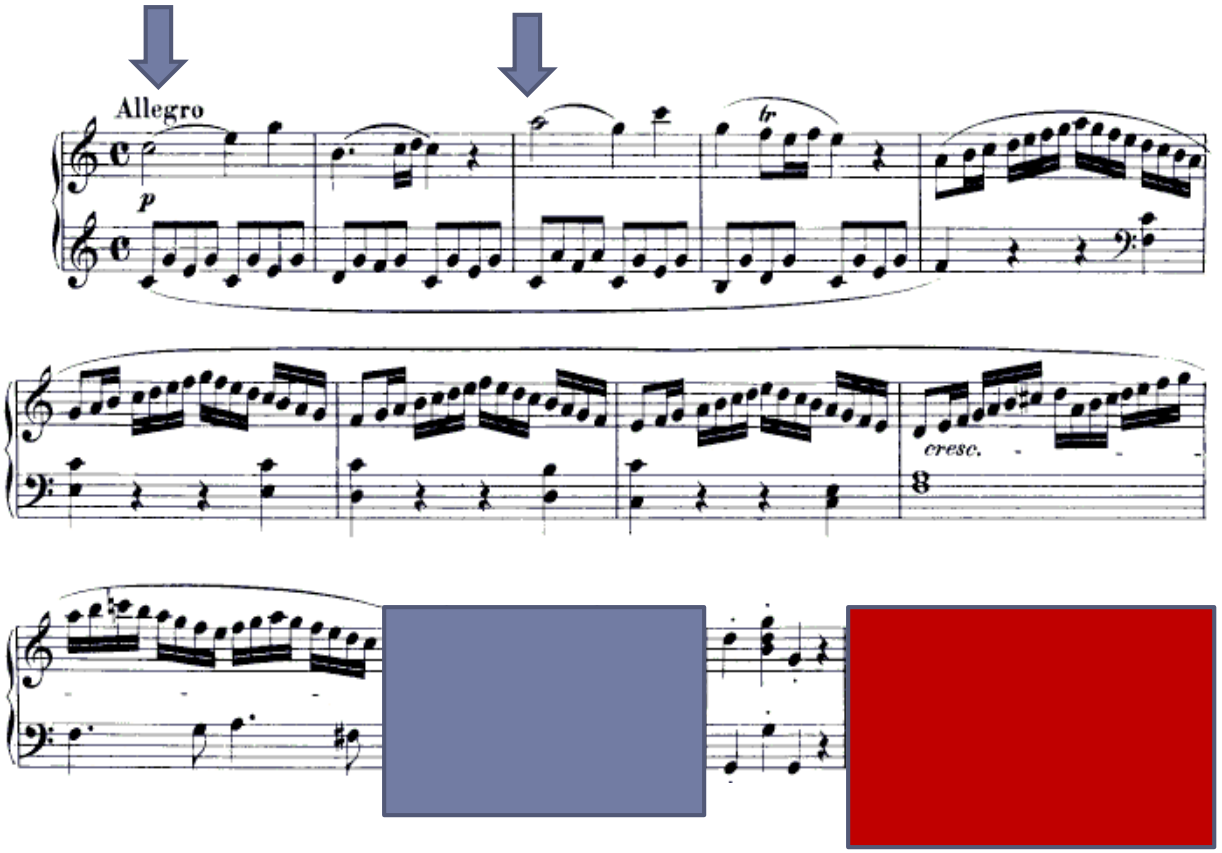


Metrical reductions



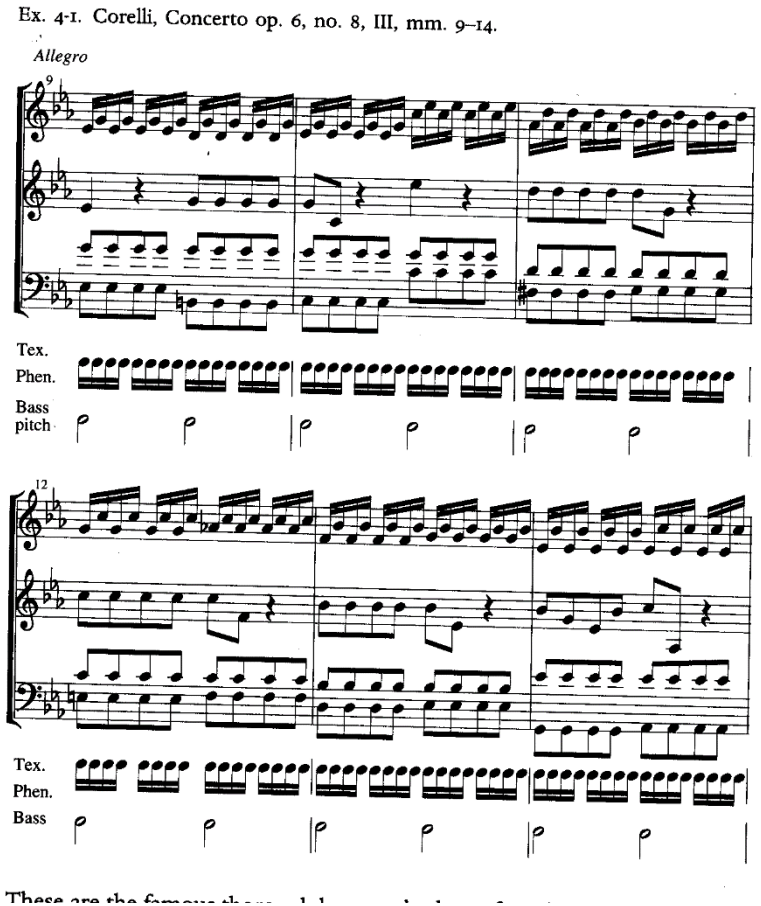
Harmonic evaluation

- Musical texture:
  - interval of assessment
  - Harmonic bald spots
  - Thematic neutrality



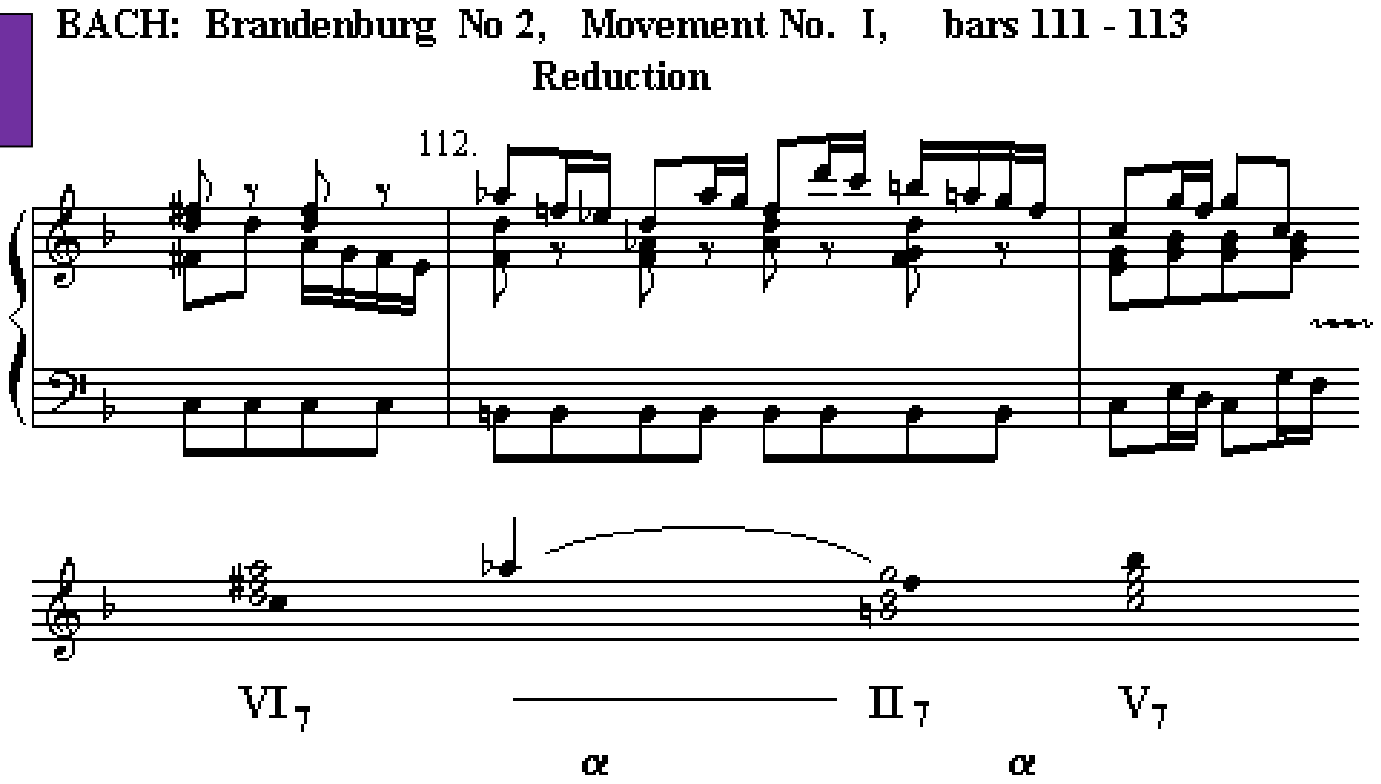
Joseph Swain: *Harmonic Rhythm* (1998)

- Six levels of harmonic rhythm
  - Phenomenal rhythm
  - Bass-pitch rhythm
  - Root analysis
  - Within-key analysis
  - Density
  - Harmonic function
  - Interpretation



Schenker (Schenkerian analysis)

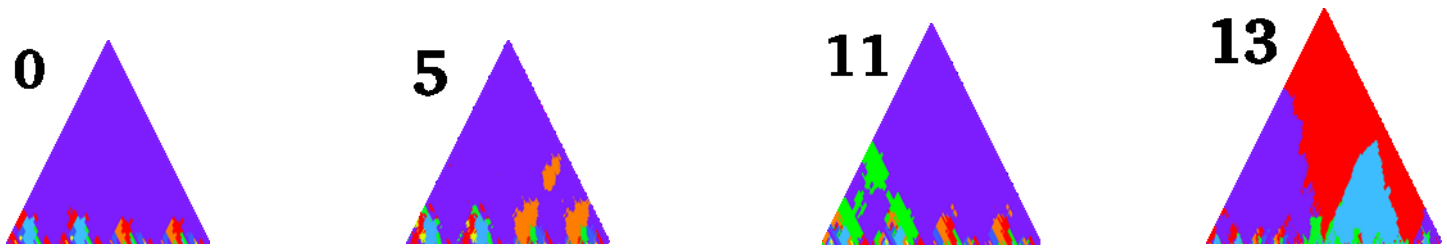
Foreground/ background



Example 3.16.

Evaluation and detection (Sapp)

- Riemannesque analysis: root-based chord analysis
  - kern > eval > new spine > gmn
  - chord quality tool (Sapp)
- Visualization of chord root/quality > key (Sapp)
- Pattern violations (#13)



Schubert: Piano Variations D 576

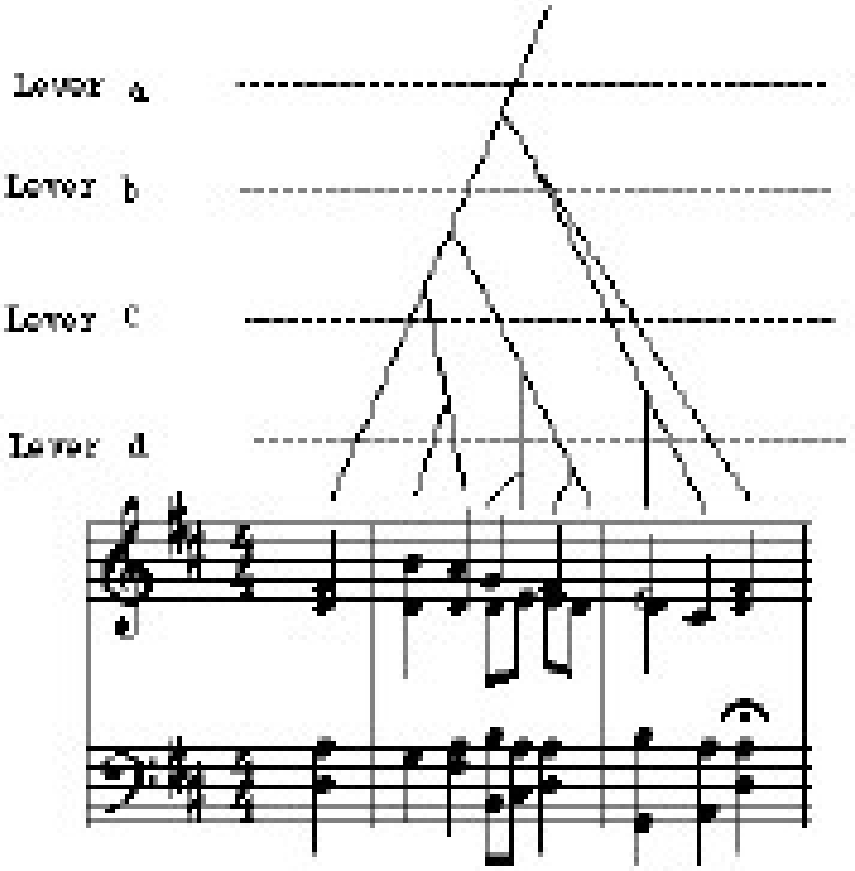
Lerdahl (Gestalt readings)

Lerdahl & Jackendoff:

Generative Theory of Tonal Music (MIT, 1983)

Grammatical structures

- Grouping structures
  - Motives, phrases
- Metrical structures
  - Strong, weak beats
- Time-span reductions
  - Tree structures
- Prolongational reductions
  - Psychological awareness



Bach chorale

Lerdahl: *Tonal Pitch Space* (2001)

GTTM rules

1. Well-formedness **rules** (structure)
2. Preference rules (listener-based)
3. Transformational rules (grouping, deceptive situations)

Preference rules

1. Harmonic tension
2. Melodic attraction
3. Attraction, expression

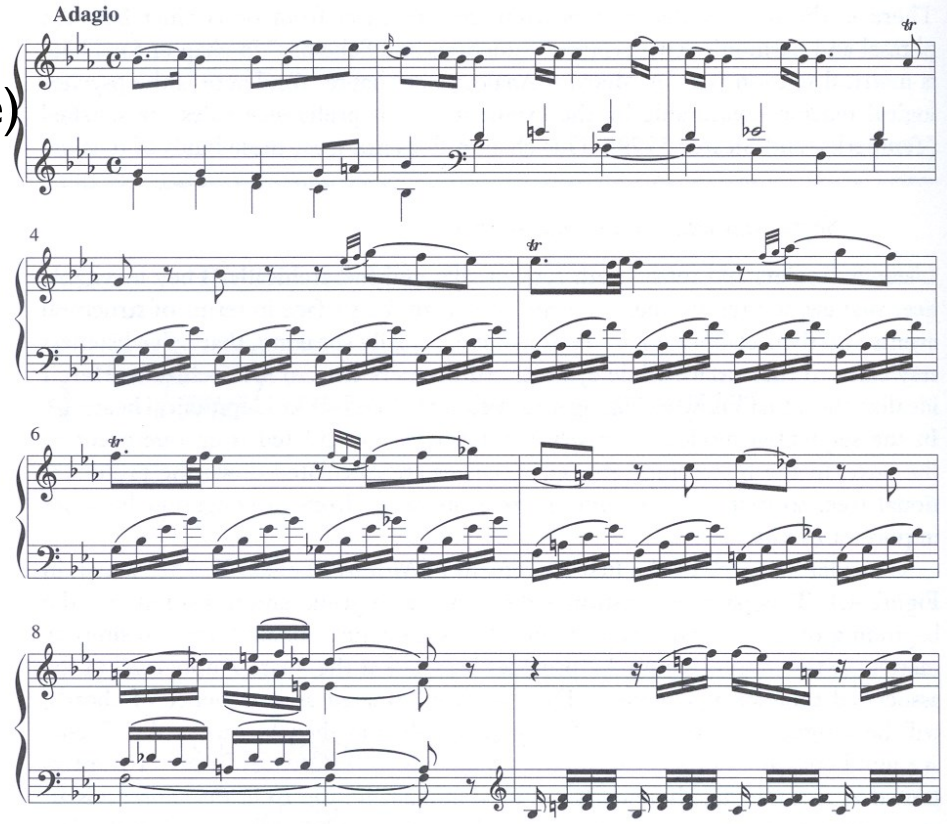


FIGURE 4.1 Mozart's Sonata, K. 282, I, bars 1–9.

Lerdahl: Tonal Pitch Space (2001)

Riemannian functions

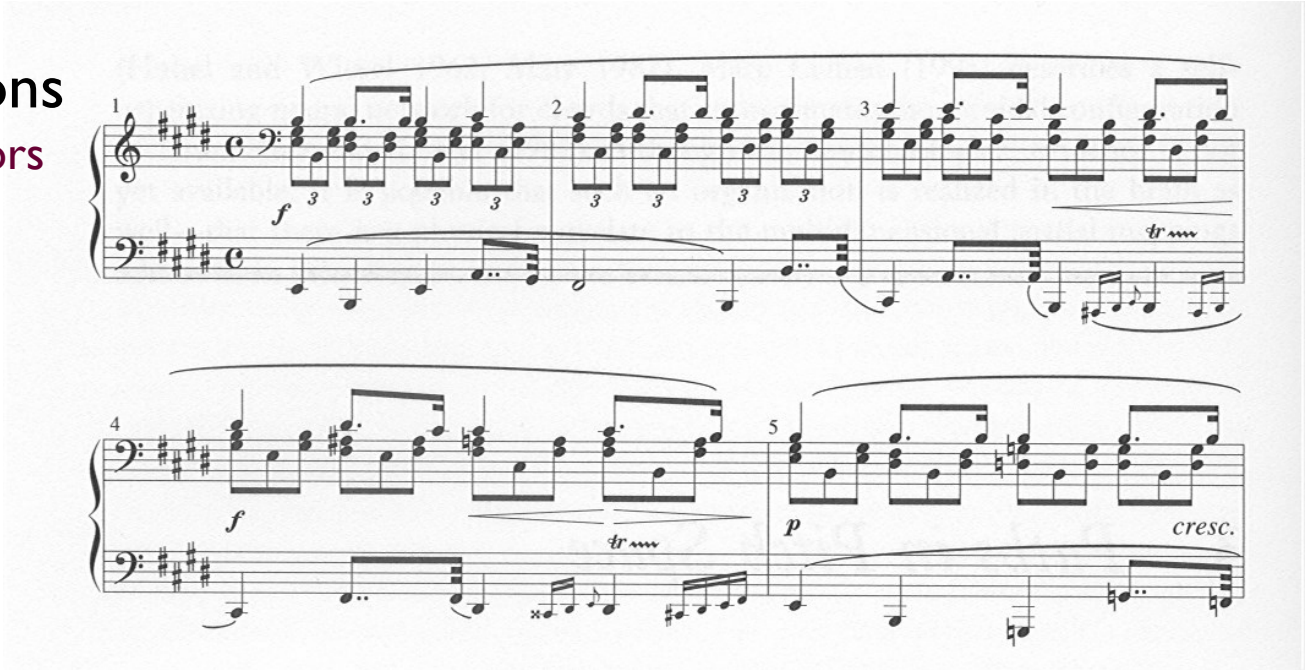
Octatonic vs hexatonic spaces

Chromatic spaces

Whole-tone spaces

Metrical attractions

Psycho-acoustical factors



Lerdahl, Krumhansl (2007), 1

"Modelling Tonal Tension," *Music Perception* 24, 329-366 (2007)

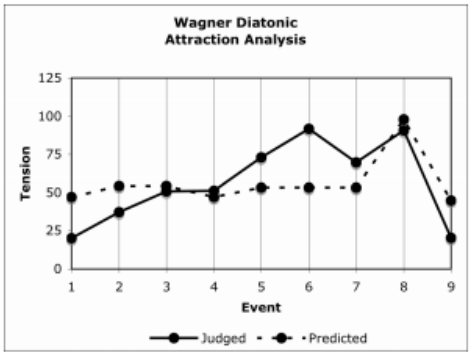


FIGURE 18. Attraction analysis of the Grail theme.

Attraction

Tension

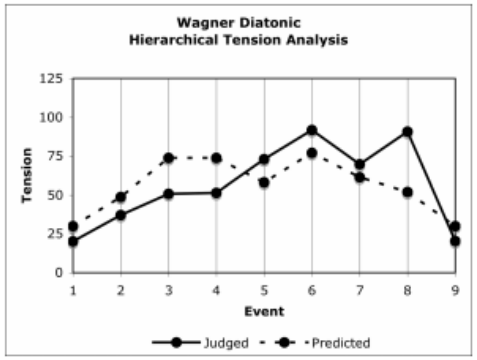


FIGURE 20. Tension graph for the theoretically preferred hierarchical analysis of the Grail theme.

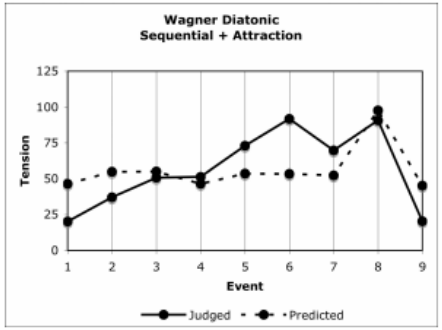


FIGURE 19. Combined sequential + attraction analysis of the Grail theme.

Combo attraction

Combo hierarchical

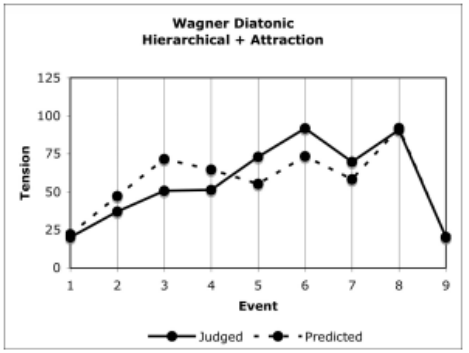


FIGURE 21. Combined hierarchical (theoretically preferred) + attraction analysis of the Grail theme.

Principles: Prolongational structure, pitch-space model, surface-tension model, attraction model--Experimental results

Lerdahl, Krumhansl (2007), 2

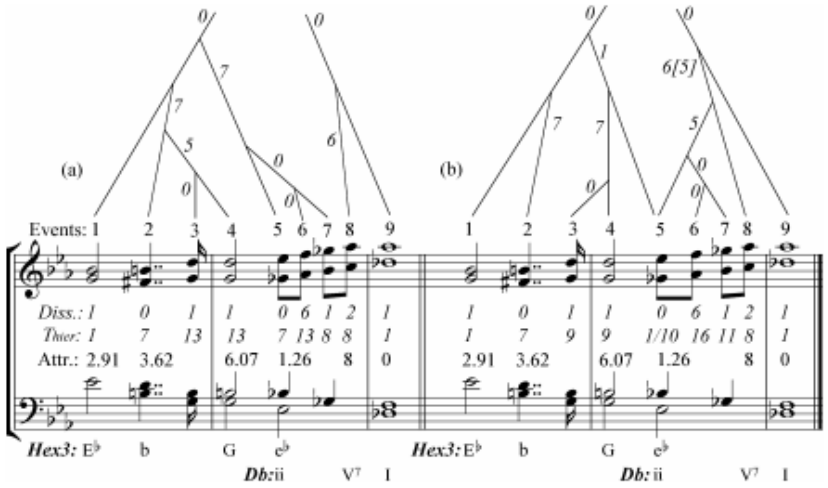
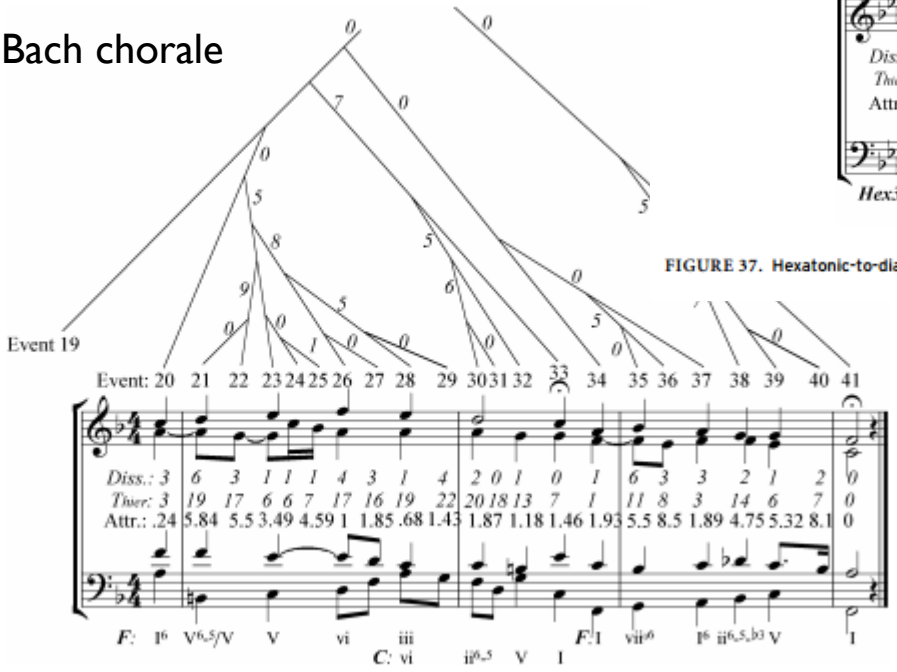


FIGURE 37. Hexatonic-to-diatonic analyses of the chromatic version of the Grail motive: (a) right-branching interpretation; (b) *TPS* interpretation.

Bach chorale



Wagner "Grail" motif.

. Analysis of the Bach chorale, phrases 3-4.

Temperley 2003, 1

Music Cognition:

The Cognition of Basic Musical Structures (2003)

Areas covered:

- Metrical structure
- Phrase structure
- Melodic phrase structure
- Contrapuntal structure
- Harmonic structure
- Key structure

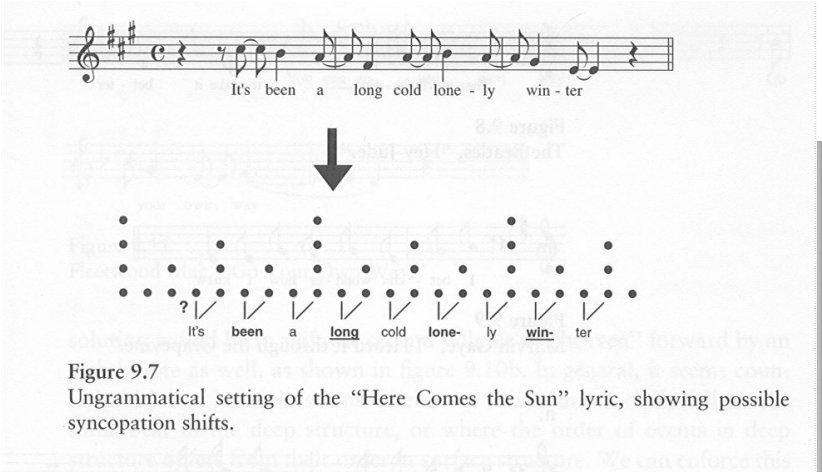
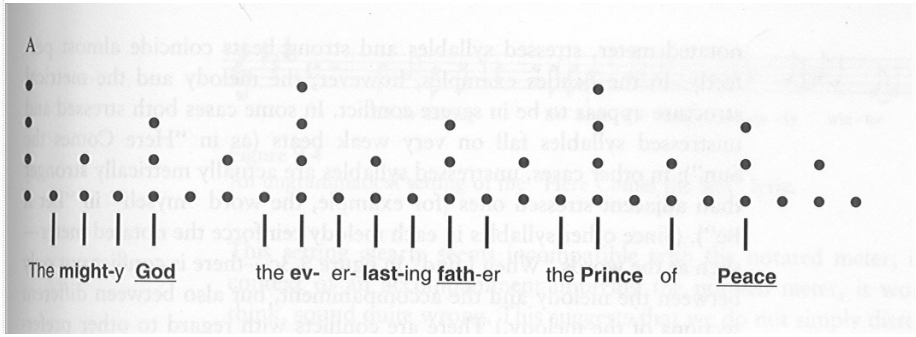


Figure 9.7
Ungrammatical setting of the "Here Comes the Sun" lyric, showing possible syncopation shifts.



Temperley 2003, 2

- Repertories and perspectives
  - Ambiguity
  - Rock
  - African music
  - Generative processes
  - Non-metrical music
  - Arbitrariness

Method: mainly based on GTTM (Lerdahl…) and extensions to it

Software: (*Melisma*): mainly written Daniel Sleator

[cf on KernScores]

Temperley (3)

- *Music and Probability* (2006)

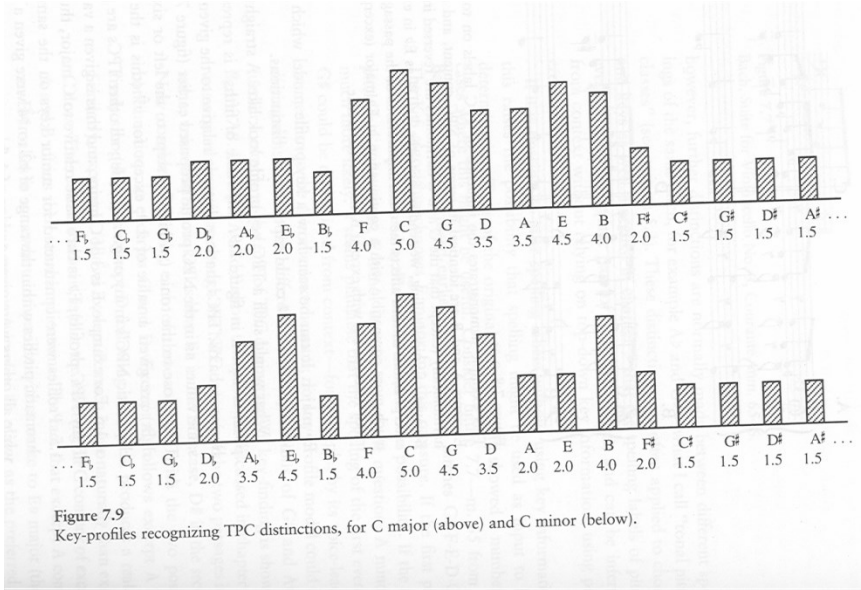


Figure 7.9
Key-profiles recognizing TPC distinctions, for C major (above) and C minor (below).

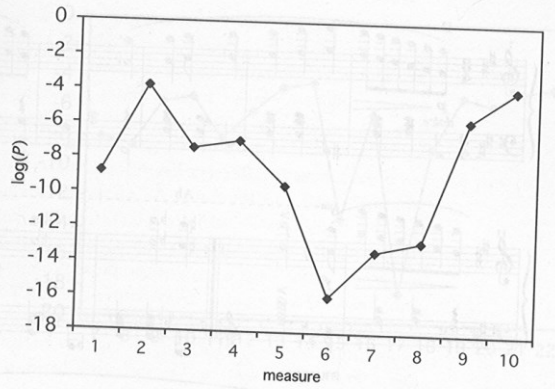


Figure 7.7
The model's probability scores for the Chopin Mazurka excerpt in figure 7.6.

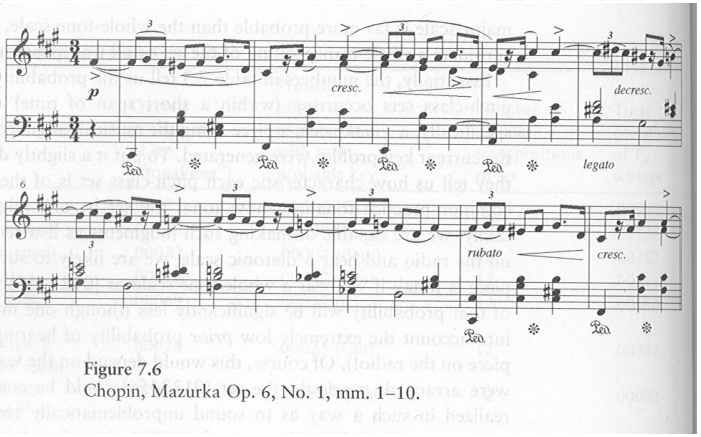


Figure 7.6
Chopin, Mazurka Op. 6, No. 1, mm. 1–10.

Harmonic generation

Generation of **harmony from melody**

Kemal Ebcioglu (SUNY Buffalo, 1986; IBM)

rule ("expert") systems

(100 for thesis,

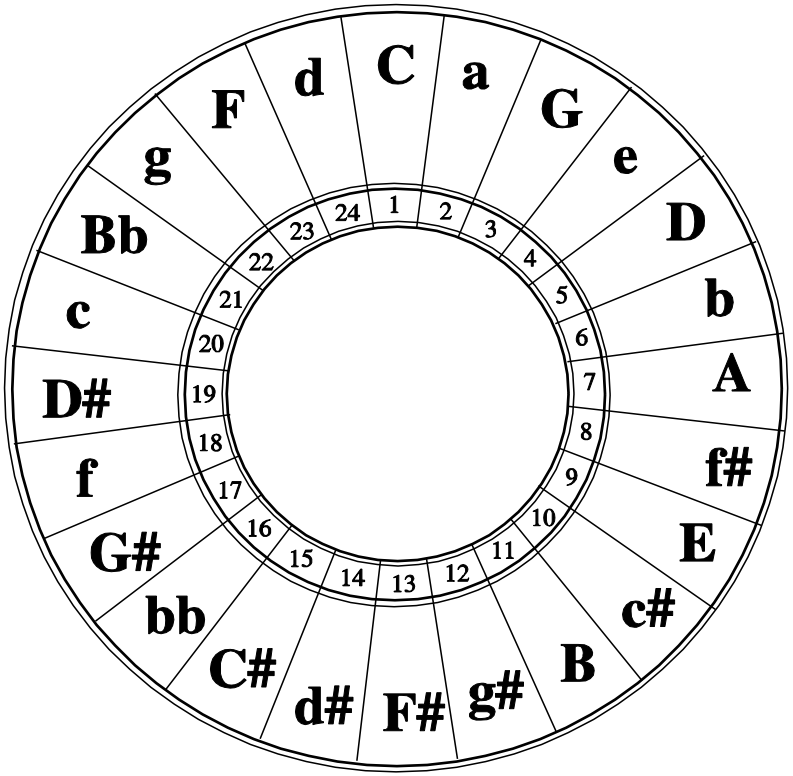
300 in post-thesis work)

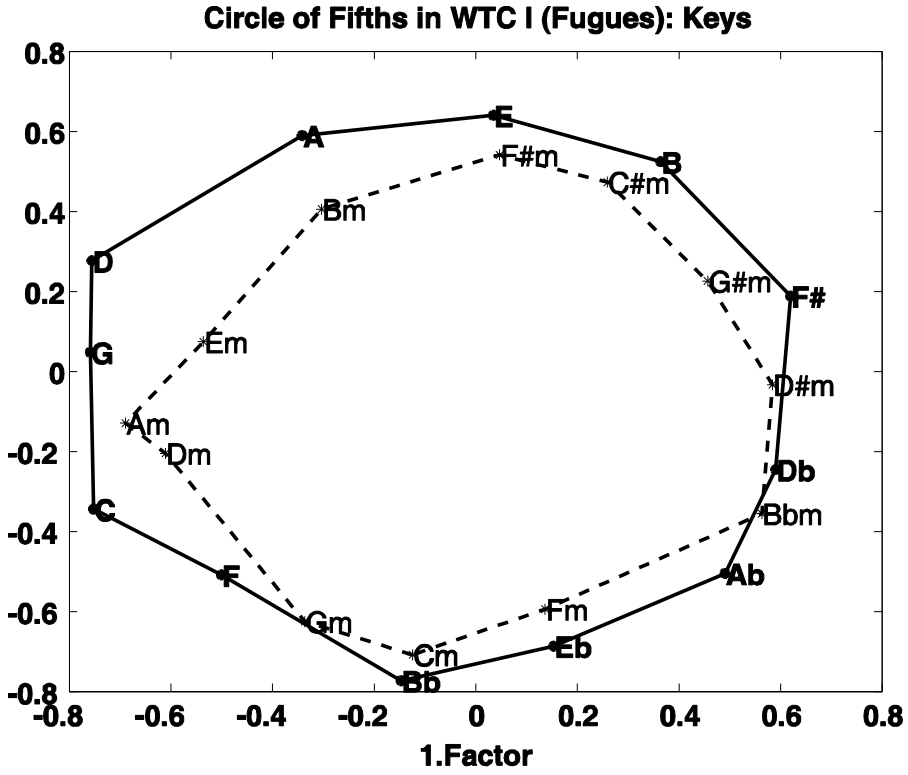
Generation of **entire chorales**

David Cope (UC Santa Cruz, 2005)

augmented transition network

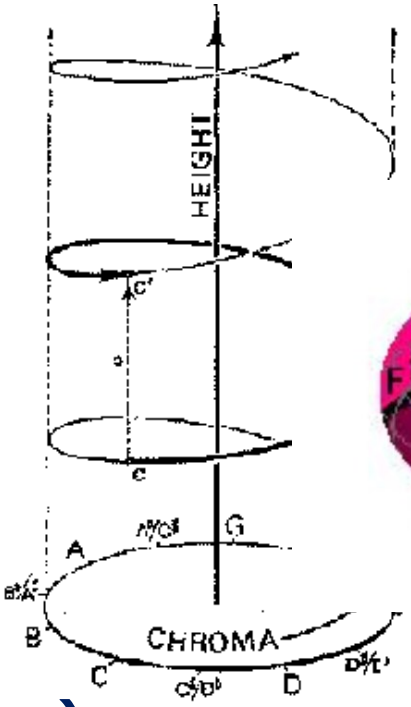
Izmirli: Acoustics vs. Circle of Fifths

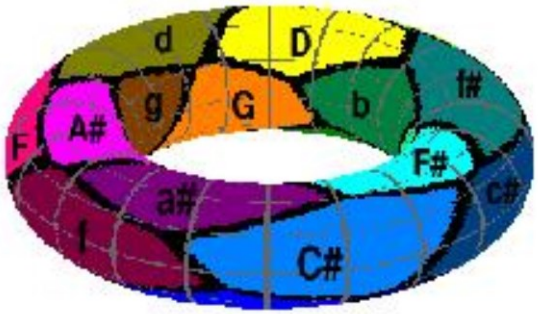




Geometrical models of tonality (2000-2010)

- 18th century
  - Heinichen
  - Euler
- 19th century
  - Riemann
- 20th century
  - **Shepard (SU)**
  - **Krumhansl (SU, Cornell)**
  - **Lerdahl (Columbia)**
  - **Chew (SU, MIT, London)**
  - **Purwins (Berlin, Barcelona)**
  - **Sapp (SU)**

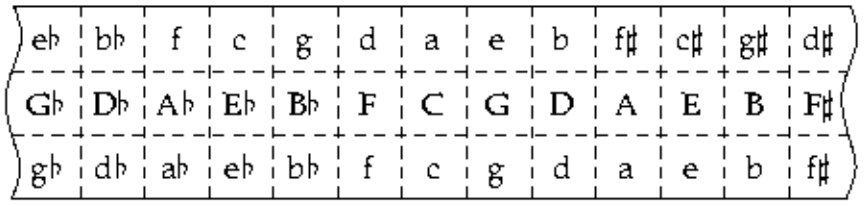


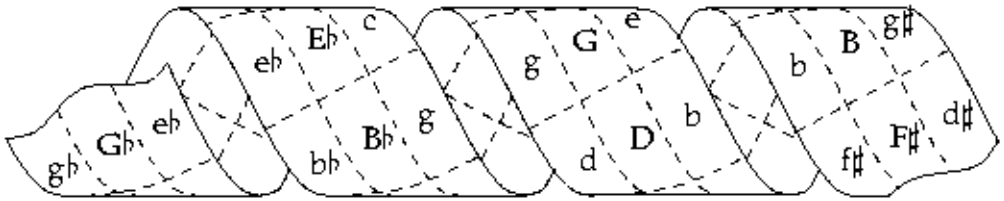


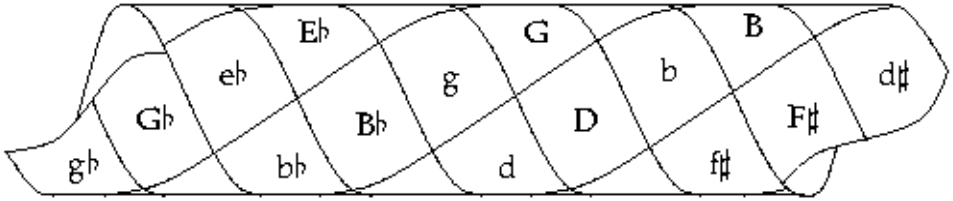
Toroidal models of tonality

G. Weber key chart

d♯	F♯	f♯	A	a	C	c
g♯	B	b	D	d	F	f
c♯	E	e	G	g	B♭	b♭
f♯	A	a	C	c	E♭	e♭
b	D	d	F	f	A♭	a♭
e	G	g	B♭	b♭	D♭	d♭
a	C	c	E♭	e♭	G♭	g♭

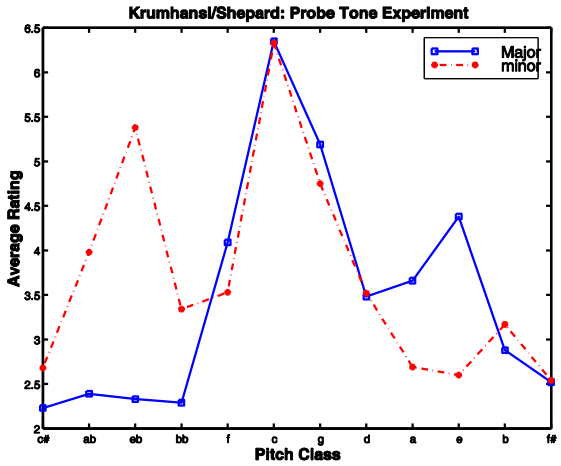




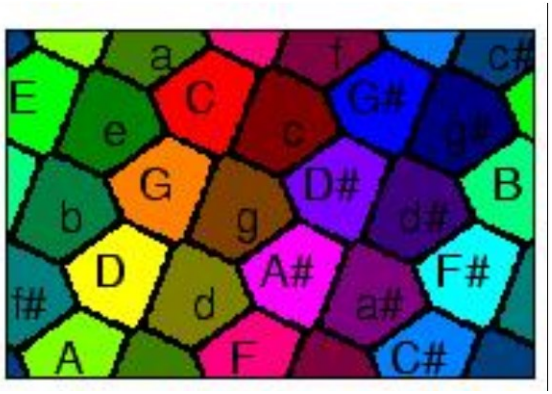


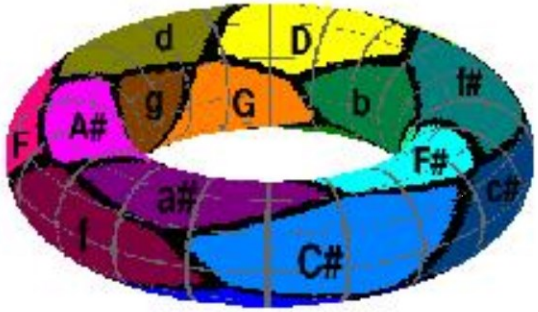
Krumhansl:
Cognitive Foundations of Musical Pitch (1990)

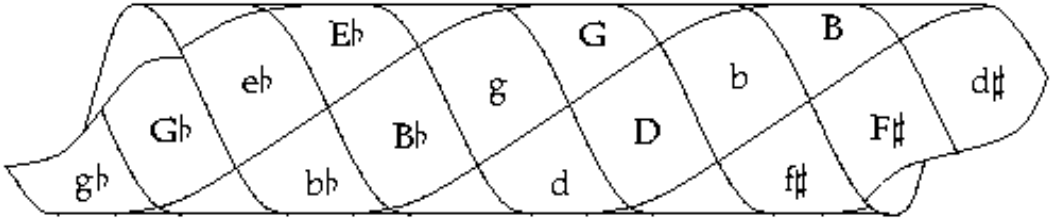
Hendrik Purwins



Stephen Malinowski

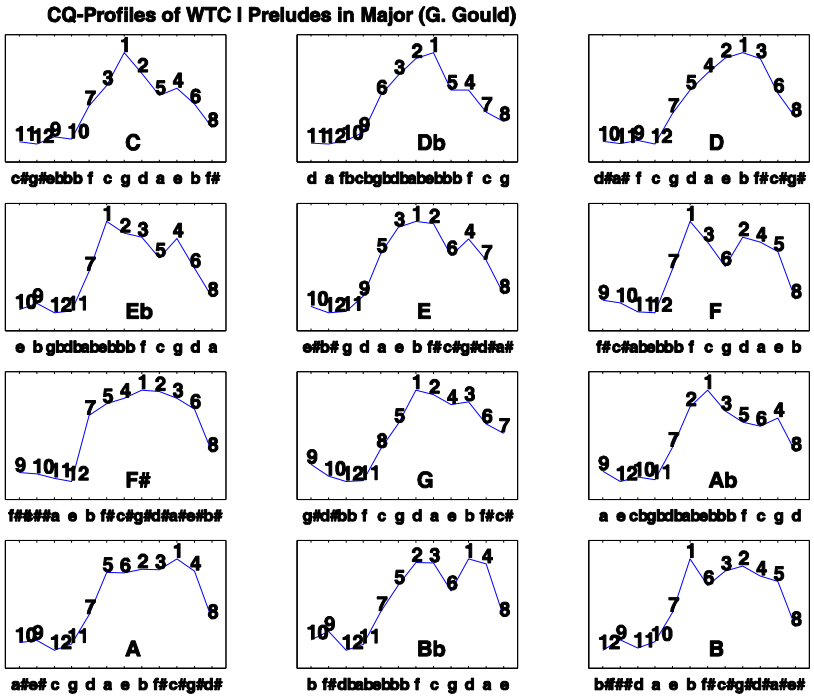


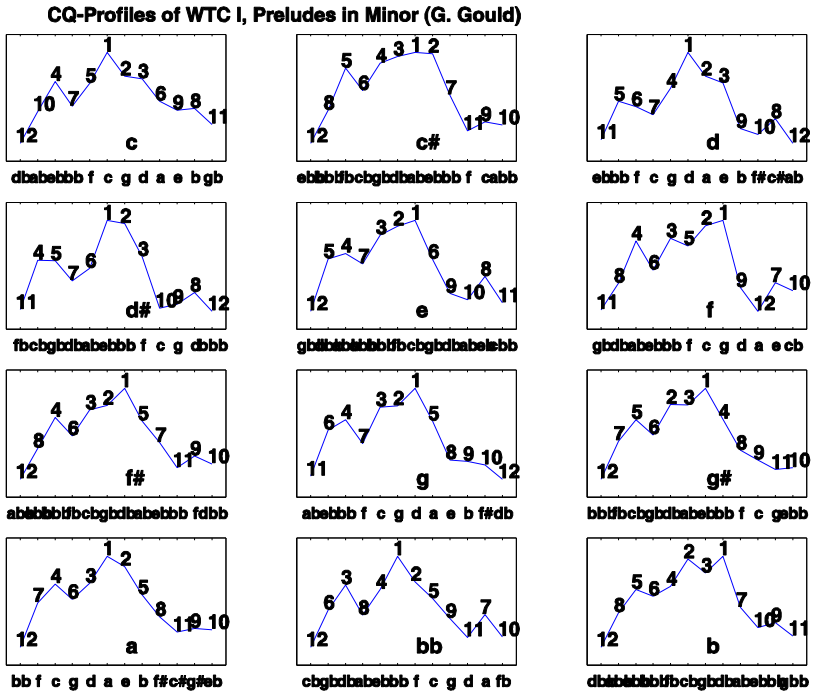




Weber

Well Tempered Clavier (Purwins)





Harmonic usage profiles of individual preludes and fugues from JS Bach's WTC (1722)